**Challenges in estimating species age from phylogenetic trees**

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**Abstract**

**Aim.** Species age, the elapsed time since origination, can give an insight into how species longevity might influence eco-evolutionary dynamics and has been hypothesized to influence extinction risk. Traditionally, species ages have been measured in the fossil record. However, recently, numerous studies have attempted to estimate the ages of extant species from the branch lengths of time-calibrated phylogenies. This approach poses problems because phylogenetic trees contain direct information about species identity only at the tips and not along the branches. Here, we show that taxon sampling, extinction, and different assumptions about speciation modes can significantly alter the relationship between true species age and phylogenetic branch lengths, leading to high error rates. We find that these biases can lead to erroneous interpretations of eco-evolutionary patterns derived from the comparison between phylogenetic age and other traits, such as extinction risk.

**Innovation.** For bifurcating speciation, which is the default assumption in most analyses, we propose a probabilistic approach to improve the estimation of species ages, based on the properties of a birth-death process. We show that our model can reduce the error by one order of magnitude under cases of high extinction.

**Main conclusion.** Our results call for caution in interpreting the relationship between phylogenetic ages and eco-evolutionary traits, and show that, under some assumptions, it is possible to obtain better approximations of species age by combining information from branch lengths with the expectations of a birth-death process.

**Key words:** Evolutionary history, Extinction rates, Incomplete sampling, Simulations, Speciation modes, Phylogeny.

**Introduction**

The estimation of species age, or the elapsed time since species origin, is important to evaluate mechanisms that link species longevity with eco-evolutionary processes (Benton, 2013; Swenson, 2019). For instance, age-dependent extinction hypotheses test the relationship between species age and extinction probability, assessing whether extinction rates differ between young and old species (Balmford, 1996; Eldredge et al., 2005; Pearson, 1995). Likewise, species age could be a measure of colonization time, especially in island systems (Tanentzap *et al.* 2015) or during biotic invasions triggered by geological events, such as the formation of the Central American Isthmus for the Great American Interchange (Carrillo *et al.* 2015, 2020). Species age is measured in the fossil record through different statistical and probabilistic approaches, based mostly on taxa’s stratigraphic duration (i.e., the time between the first and last appearance of a taxon in the fossil record) (Foote, 1996; Foote & Raup, 1996). Several of these approaches consider differences in fossil sampling and temporal resolution (Alroy et al., 2001; Silvestro et al., 2019). Species ages estimated from paleobiological data offer a reliable measure of species’ temporal duration which can be used in macroevolutionary studies (Benton, 2016; Silvestro et al., 2020; Van Valen, 1973). More recently, several studies have used the length of terminal branches in time-calibrated phylogenies as a proxy for the age of extant species, an approximation that we hereafter refer to as “phylogenetic age” (Alzate et al., 2023; Davies et al., 2011; Gaston & Blackburn, 1997; Johnson et al., 2002; Pie & Caron, 2023; Sonne et al., 2022; Tanentzap et al., 2020; Verde Arregoitia et al., 2013). These phylogenetic ages have been used as the basis to test for links between species age and current extinction risks (Tanentzap et al., 2020; Verde Arregoitia et al., 2013) and to assess various correlations with evolutionary, biogeographical, and ecological patterns in living species (Alzate et al., 2023; Freer et al., 2022; Kennedy et al., 2022; Pie & Caron, 2023)

While several studies have used phylogenetic age at face value for species age (e.g., Johnson et al. 2002; Tanentzap et al. 2020; Verde Arregoitia et al. 2013), their potential deviation from the true species ages remains unclear. Specifically, we identify three non-mutually exclusive shortfalls that can lead to over- or underestimation of species ages. First, incomplete sampling of extant species, either due to incomplete species sampling or linked to species still being unknown to science, can bias phylogenetic age estimation by artificially increasing the length of terminal branches (Heath et al., 2008; Mynard et al., 2023).

Second, extinction events will mask branching events in phylogenetic trees of extant species (Harvey et al., 1994; Nee & May, 1997). Even in phylogenetic trees that include extinct taxa, the incompleteness of the fossil record will inevitably lead to missing lineages and incorrect topologies. Unsampled extant and extinct species from the phylogeny results in an inflation of the length of terminal branches leading to sampled species (i.e., the tips of the tree), thus altering phylogenetic species ages. For instance, if the extinct species of the *Homo* genus are not included in a phylogeny, the phylogenetic age of *Homo sapiens* is approximately 10 million years, i.e., the age of the last common ancestor with its sister species, the chimpanzee (Rivas-Gonzáles et al. 2023). This estimate exceeds the age of the oldest known fossil of modern humans (i.e., *Homo sapiens*) by two orders of magnitude (Fig. 1; Callaway 2017).

The third shortfall, is that the tree alone does not contain information about the underlying speciation mode and does not include species labels along its branches, such that only the tips can be unequivocally assigned to a named species (Losos & Glor, 2003). Alternative speciation modes have been discussed in the literature reflecting different biological processes and species concepts, including bifurcating, budding, and anagenetic speciation (Foote, 1996; Silvestro et al., 2018). These modes define the relationship between the ancestral species and its descendants, thus contributing to determining species ages (Rosenblum et al., 2012; Wagner, Erwin, & Anstey, 1995) (Fig. 2). Most phylogenetic trees are depicted in the rectangular shape, where the two descending lineages split symmetrically from an ancestral lineage, thus suggesting a bifurcating speciation mode where two new species replace the ancestral lineage (Baum et al., 2005; Caetano & Quental, 2022). However, the often-unstated assumption of virtually all birth-death processes used to model phylogenetic branching times, is that speciation occurs as a budding process, with a speciation event leading to a single new species and the survival of the parent species, even though we cannot determine which descendant branch is the new species (Gernhard, 2008; Nee et al., 1994; Stadler, 2013). Anagenetic speciation, in contrast, does not lead to a branching event and is therefore not ordinarily visible on a phylogenetic tree.

All speciation modes may reflect plausible biological processes, and evidence for each mode has been found in the fossil record (Foote, 1996; Simpson, 1984) and in extant species (Skeels & Cardillo, 2019). Under bifurcating speciation mode, phylogenetic ages equal species ages when there is no extinction, and all species are sampled. A phylogenetic tree, under budding speciation, typically lacks information about which of the two descendent branches is the new species after a speciation event (but see Aze *et al.* 2011). Thus, in the absence of extinction, the phylogenetic age of one sister species will equal its species age while the other will be older but without the possibility to identify which one is which. Anagenetic speciation is not associated with a branching event but can be used to describe different species or morphospecies (Emerson & Patiño, 2018) delimited by substantial phenotypic change occurring along a lineage (Roopnarine et al., 1999) and will cause a higher phylogenetic age than the genuine species age.

Here we use simulations to quantify the predictability of species age from phylogenetic trees of extant taxa, under different diversification scenarios. Specifically, we performed simulations where we know the true age of species to: 1) quantify the error in phylogenetic ages under various scenarios combining different speciation modes with a range of speciation and extinction rates and incomplete sampling; 2) examine whether this error affects our ability to make qualitative decisions on the order of species ages; 3) explore whether the signal of age-correlated extinction risk is preserved in the phylogenetic age of species. Finally, we propose a new method to estimate species age more accurately under the assumption of bifurcating speciation and complete extant species sampling, which are the most widely used assumptions in eco-evolutionary studies (e.g., Alzate et al., 2023; Tanentzap et al. 2020), and assess its ability to improve our interpretation of age-dependent extinction risks.

**Methods**

*Simulating species ages*

We generated complete phylogenies of extant and extinct species under a stochastic birth-death process using the package TreeSim 2.4 (Stadler, 2010) for the R 4.3.0 statistical programing environment (R Core Team 2023). Then we mapped species on the complete phylogenies using the R package FossilSim 2.3.1 (Barido-Sottani et al., 2019) under different speciation modes, thus assigning species labels across all branches of the tree. We used the labels assigned to terminal extant taxa to determine the true species ages. We then dropped all extinct species from the tree and obtained the length of terminal branches, to quantify the phylogenetic age of extant species. Finally, we rescaled all phylogenetic trees to a root age of one, which ensures that the absolute errors in species ages are comparable in plots, and compared the relative true and phylogenetic ages among different simulation scenarios.

*Error in equating phylogenetic and species age*

To explore whether there is a consistent over- or underestimation of species ages and to quantify error in approximating species ages with phylogenetic ages, we simulated a range of datasets with different speciation modes and diversification rates. First, we simulated 3 sets of 100 phylogenetic trees with 100 extant species based on speciation rates equal to 0.1, 0.5, and 1, combined with 100 extinction rates ranging from 0 to 0.99 in equal increments (Beaulieu & O’Meara, 2016). Second, on each of these phylogenies we mapped species according to different scenarios of speciation: (1) budding speciation, (2) bifurcating speciation, (3) a combination of budding speciation and anagenetic speciation with the rate of anagenesis set to half of the speciation rate, and (4) bifurcating speciation combined with anagenetic speciation with the rate of anagenesis set to half of the speciation rate.

Across all trees, we obtained in total 120,000 extant species, 30,000 for each speciation scenario. For each speciation mode and extinction fraction rate (defined as death/birth Beaulieu & O’Meara, 2016), we calculated the mean absolute percentage error (MAPE) across all species for each tree as measure of the deviation between the phylogenetic ages from the true age:

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where *s* is the true species age, *v* is the phylogenetic age, and *n* is the number of tips in the tree (pruned of the extinct species).

Next, for each speciation mode, we plotted the MAPE against the simulated extinction fraction.

*Impact of age error in comparing species ages*

To explore whether the error introduced by approximating species age with phylogenetic age impacts our ability to make qualitative judgements, such as which of two extant species is the younger one, we simulated 1,000 phylogenetic trees with values of extinction fractions (extinction rate divided by speciation rate) of 0.9, 0.5, and 0, combined with a fixed speciation rate of 1 (3000 trees). Second, on each of these phylogenies, we mapped species according to budding and bifurcating speciation. Thus, we simulated 300,000 extant species for each speciation mode. Next, we calculated the proportion of cases where the younger of two species, according to its phylogenetic age, is, in fact, the older one given the true age of the two species. We performed this comparison from the perspective of an empirical researcher that can only obtain the phylogenetic ages. We made two types of comparisons for each phylogeny: (1) between the youngest and oldest species in the phylogeny, and (2) between two randomly selected species.

*Error in the phylogenetic age due to uniform incomplete sampling*

We used the intermediate extinction scenario with an extinction fraction of 0.5 to explore the error in equating phylogenetic and true age that is introduced by uniform incomplete sampling under the scenarios of bifurcating and budding speciation. We specified a fully sampled phylogeny, with 25% or 50% incomplete sampling. We simulated trees conditioning on the total tip number, such that they included 100 sampled tips, i.e., after dropping the unsampled ones (134 or 200 total tips). We calculated the MAPE for each tree and compared the incomplete sampling scenarios for each speciation mode.

*A probabilistic method to infer species age*

Under the assumption of bifurcating speciation and complete sampling, the phylogenetic age represents the upper boundary of plausible species ages and corresponds to the true age in the absence of extinction. However, the true age could be younger if extinction led to the disappearance of recent cladogenetic events from the phylogeny of extant species. Given a phylogenic age *vi* the probability that the true species age *si* is exactly *vi* is conditional on no other speciation or extinction event having occurred between *vi* and the present. We approximate the probability of no speciation or extinction for an arbitrary small time bin *t* based on the probability that a lineage results in a single descendant, which is (Kendall, 1946):



based on a birth-death process with time-homogenous speciation rate λ and extinction rate μ. The probability that no event occurs over a time window *v, i.e.,* until the age of the observed node *i*,is approximated as:



In the absence of extinction (μ = 0), the probability of the true species age *si* to be equal to *vi* is 1, because any speciation event following the node *vi* would be observed in the tree of extant species. Thus, we calculate the normalized probability of the speciation event to occur at time *vi* as:

 (1)

We then compute the probability of a speciation time for any given time *τ* as:

, (2)

where the first term quantifies the probability of the species age along a vector of times, while the second term normalizes it after accounting for the probability that speciation occurred exactly at the node. We use equations (1) and (2) to approximate a density describing the probability of a species origination at the observed phylogenetic age and along the branch connecting the node with the tip. As point estimates of the species age, we tested whether the mean or the median of the distribution better approximate the true species age compared to the phylogenetic age.

To evaluate the accuracy of our probabilistic species age estimator, we simulated 1,000 phylogenetic trees with extinction rates of 0.25, 0.15, and 0.05, and a fixed speciation rate of 0.3. Using these phylogenies as inputs, we mapped species on each tree based on a bifurcating speciation process. Then, we calculated the MAPE for each tree as a measure of the deviation between the function’s estimated and the phylogenetic ages from the true age.

*Simulation of age-dependent species extinction risks*

To evaluate the impact of the erroneous estimation of species age due to the extinction shortfall on macroevolutionary analyses, we explored whether the assumed relationship between species age and contemporary extinction risk (e.g., Johnson et al. 2002; Tanentzap et al. 2020; Verde Arregoitia et al. 2013) is preserved in the phylogenetic ages. For this, we binned the same number of extant species according to their age in five categories reflecting the increase in extinction risk with age encapsulated by the IUCN categories: Least Concern (LC), Near Threatened (NT), Vulnerable (VU), Endangered (EN), and Critically Endangered (CR; International Union for the Conservation of Nature 2016). With this, we generated a positive effect with older species being at higher extinction risk regarding the IUCN categories, assuming bifurcating speciation.

Then, we quantified the share of the 1000 datasets where the order of the mean age per IUCN category did not match with the simulated monotonic increase when utilizing (a) phylogenetic ages, and (b) the probabilistic species age estimator. We also evaluated the effect of nonrandom incomplete sampling (older species were less prone to be sampled than younger ones) on the evaluation of species age-correlated extinction risks.

**Results**

*Error in equating phylogenetic and species age*

Under the assumption of bifurcating speciation and with no extinction events, phylogenetic ages matched the true age of extant species (Fig. 3). At low extinction fractions (< 0.25), 96% of the phylogenetic age estimations were congruent with the true age. At higher extinction fractions (> 0.75), this was also the case for most species (73%). However, age overestimation increased with extinction fraction and in some cases the phylogenetic age erroneously suggested that the species is as old as the root age. While under bifurcating speciation, the phylogenetic age never underestimated the true species age, both over- and underestimation occurred in the case of budding speciation. Moreover, the proportion of cases where the phylogenetic ages equal the species age was lower than in the bifurcating scenario (Fig. 3). Overestimated ages were more frequent with high extinction while underestimations occurred with low extinction, but in principle both happened under the complete range of extinction rates (Fig. 3). Even at low extinction fractions, ~50% of phylogenetic ages did not match the true ages.

In datasets simulated under a mixture of anagenetic and bifurcating speciation, phylogenetic ages deviated more strongly from the true ages than under a pure bifurcating process, given that anagenetic events are unobserved in the phylogeny (Fig. SM1). With a low extinction fraction, phylogenetic ages were congruent with the true species ages in 78% of the cases instead of 96%, and with high extinction the share decreases from 73% to 62%. Datasets with mixed anagenetic and budding speciation, phylogenetic ages also deviated more that under a pure budding process; with a low extinction fraction, phylogenetic ages were congruent 40% instead of 50% of the time, and with high extinction the accuracy decreased to 34%.

While a budding speciation mode led to a higher baseline error than bifurcation, the latter showed a stronger increase with extinction (Fig. 4). Under both modes of speciation, speciation rates did not have a substantial impact on error in age. For strictly bifurcating speciation, there was no error in the absence of extinction, but the MAPE increased to up to 150% with extinction fractions exceeding 0.75. In contrast, under budding speciation the MAPE was around 25% in the absence of extinction, increasing to 30-120% with extinction fractions exceeding 0.75. In datasets that included anagenetic speciation, the MAPE reached as high as 500% in some simulations (Fig. SM2).

*Impact of age error on comparing species ages*

For the combination of strictly bifurcating speciation and all extinction scenarios, selecting the phylogenetically youngest and oldest species never resulted in a case where the presumed older species has been in fact the younger of the two species according to their simulated age (Fig. SM3a). Thus, for this speciation mode, the risk of a qualitative error when comparing species at the extremes of the age range is minimal. However, the age ranking of two randomly selected species was found to be incorrect in 6% and 8%, for intermediate and high extinction, respectively (Fig. SM4a). Thus, qualitative errors in comparing species ages are non-negligible under the assumption of bifurcating speciation.

In contrast, for budding speciation, the age rank of the oldest and youngest species was erroneously determined in 2.2% of the simulations in the absence of extinction, increasing to 7.5% and 12.2% for intermediate and high extinction, respectively (Fig. SM3b). Thus, under the assumption of budding speciation, there is a substantial risk of mistaking the oldest and youngest species in the clade. The error in age ranking of two randomly selected species was even higher, exceeding 25%, irrespective of the extinction level (Fig. SM4b).

*Error on equating phylogenetic and species age given uniform incomplete sampling*

Under bifurcating speciation, the MAPE for completely sampled trees was 25 ± 20%; for trees missing 25% of the extant species the error increased by 15 orders of magnitude; and for trees missing 50 % of the extant species the error increased by 85 orders of magnitude (Fig. 5a). Under budding speciation, the MAPE for completely sampled trees was 42 ± 15 %; for trees missing 25 % of the extant species the error increased by 5 orders of magnitude; and for trees missing 50% of the extant species the error increased by 22 orders of magnitude (Fig. 5b).

*Probabilistic species age estimation*

With increasing extinction, our probabilistic estimation of species ages resulted in an increasingly lower error compared with the phylogenetic age (Figs. 6, SM5). Under low extinction the MAPE was slightly worse compared to the use of phylogenetic ages (ΔMAPE = 2.83 ± 3.9 % when using the mean of the estimated ages and 2.1 ± 1.3 % for the median across estimates). While with increasing extinction rates the MAPE of the phylogenetic ages increased up to 25% (Fig. SM5), the probabilistic estimation strongly reduced the error compared with phylogenetic age (ΔMAPE = -27 ± 26 % for the mean estimated ages and -32 ± 28 % for the median across estimates; Figs. 6, SM5).

*Detecting age-dependent extinction risk*

The use of phylogenetic age as an approximation of species age led to error rates of 1.3, 7.2, and 18.6 % in detecting the correlation between species ages and extinction risk for scenarios with low, intermediate, and high extinction rates, respectively (Fig. 7). Thus, even under intermediate extinction the true relationship between age and extinction risk was wrongly estimated in a significant fraction of the simulations, and higher extinction rates led to a further substantial drop in the reliability of this approach. In contrast, estimating species ages based on our probabilistic method led to much lower error rates (3 to 4-fold) that dropped to 1.3% and 4% with intermediate and high extinction, respectively. Under incomplete taxon sampling, in which the sampling probability was negatively correlated with species age, the error rates increased to 12.8%, and 49.5% for scenarios with 25%, and 50% of missing extant species, respectively (Fig. SM6).

**Discussion**

The use of branch lengths of phylogenetic trees as an approximation of species ages is becoming central to an increasing number of studies that use them to evaluate the relationship among macro-ecological and evolutionary patterns and current extinction risks (Pie & Caron, 2023; Sonne et al., 2022; Tanentzap et al., 2020; Verde Arregoitia et al., 2013). Here we showed that this approximation leads to substantial errors and that its accuracy is hampered by three shortfalls: unobserved extinction events, unknown speciation mode, and incomplete sampling of extant species. The only instance in which phylogenetic ages correctly predict species age is under the assumption of a bifurcating speciation process in the absence of extinction and with all living species included in the phylogenetic tree. While the prevalence of true speciation modes remains difficult to estimate (Bapst & Hopkins, 2017; Silvestro et al., 2018; Wagner et al., 1995), the fossil record unequivocally shows that extinction occurs across all clades in the tree of life (Bambach 2006; Benton 2023; Pimm et al., 2014), and there is substantial evidence that many living species remain unknown to science and are therefore absent from empirical phylogenetic trees (Blackwell 2001; Mora et al., 2011). Thus, the scenario under which phylogenetic age correctly predicts species age is very unlikely.

Some authors acknowledged the problems associated with measuring species age from phylogenies (Swenson, 2019), and have proposed approaches to account for them. For example, Sonne *et al.* (2022) determined young and old Andean hummingbirds by assessing the sensitivity of their results to incomplete taxon sampling by generating 1000 trees with randomly missing species. Pie & Caron (2023) accounted for taxonomic incompleteness by pruning an additional 1 – 5% of species and evaluated if their conclusions changed and found that they did not. Yet, the magnitude of the error associated with the direct use of the length of phylogenetic branches as estimators of species ages remains under-appreciated, as shown by the many studies implementing this approach.

We showed that the largest error in estimating species ages from phylogenetic trees is linked with incomplete sampling of extant species. This is a problem that in principle can be solved by extending the scope of the sampling to include all species in the phylogenetic inference. Yet, despite the advances in the scalability of DNA sequencing, this remains impractical for large clades, including some of the best sampled ones such as vertebrate groups, in which many species still lack genetic data (Jetz & Pyron 2018; Tonini et al., 2016; Upham et al., 2019). In addition, a substantial proportion of species might be missing from the phylogenetic trees because they are still unknown to science, a problem often identified as the Linnean shortfall (Diniz Filho et al., 2023; Hortal et al., 2015). The magnitude of the Linnean shortfall is unknown, but available estimates show that it affects some clades significantly more than others (Moura & Jetz 2021; Ondo et al., 2023), with the diversity of highly diverse groups, such as insects and fungi, likely to be highly underestimated (Blackwell 2001; Mora et al., 2011).

Our simulations showed that under some scenarios the accurate estimation of species ages is essentially impossible from phylogenetic trees using current approaches. Under the assumption of budding speciation, the error is high even without extinction and with complete sampling, because phylogenetic trees are agnostic about parent and descendant species following a branching event (Fig. 2, 4). Phylogenetic ages are, by construction, identical for sister species, which is necessarily wrong within a budding speciation scenario. Similarly, anagenetic speciation also leads to high error, which did not vary substantially with extinction. However, anagenetic speciation might be impossible to quantify, except perhaps in high resolution fossil time series (Aze et al., 2011), resulting in a general debate on the use of the term anagenesis in evolutionary biology (Vaux et al., 2015) and biogeography (Emerson & Patiño, 2018; Meiri et al., 2018). Thus, species age is unidentifiable under the assumption of speciation modes that deviate from a strictly bifurcating scenario.

The lowest error in species age estimation was observed under scenarios of bifurcating speciation. This is the implicit assumption of most studies using approximations of species ages (Alzate et al., 2023; Freer et al., 2022; Kennedy et al., 2022), even though it is at odds with the assumption of all birth-death models used in the molecular clock analyses that estimate the phylogenetic trees in the first place (Gernhard, 2008; Nee et al., 1994; Stadler, 2013). Despite the lower error, our simulations showed that both extinction and missing lineages can lead to a substantial decrease in accuracy (Fig. 4-5, SM3-4) that can even lead to qualitative misinterpretations of general patterns such as age-dependent extinction risks (Fig. 7). Given the large inaccuracy in phylogenetic age, the question is whether this affects the inferences made from the relationship between species age and eco-evolutionary variables, such as extinction risk, range size, or environmental variables (Gaston & Blackburn 1997, Johnson *et al.* 2002, Tanentzap *et al.* 2015, Pie & Caron 2023).

We found our probabilistic approach to efficiently reduce the biases associated with extinction. It substantially improved the accuracy of the estimation of species ages, leading to much lower error rates even under scenarios of high extinction fractions. The performance of our estimator is however contingent on the ability of birth-death models to correctly estimate speciation and extinction rates from completely sampled phylogenies of extant species. The accuracy of these methods has been shown to be high under several simulation settings (Silvestro et al., 2011; Stadler 2011), but their accuracy has been questioned for empirical datasets and under complex models with rate variation (Louca & Pennell 2020; Rabosky 2010). One commonly observed pattern is the estimation of 0-extinction rate from empirical phylogenies (Louca & Pennell 2021), which would make corrected ages identical to the phylogenetic ages. Yet, the fossil record decisively shows that extinction and speciation rates vary within the same order of magnitude across virtually all clades (Parry 2021). The robustness of estimated extinction rates can be increased through the use of fossil data in the analyses (Heath et al., 2014; Silvestro et al., 2018; Warnock et al., 2020). Alternatively, our probabilistic approach could be applied across a range of plausible values of speciation and extinction rates as a way to evaluate the robustness of conclusions drawn from the patterns of estimated species ages.

**Conclusion**

This study provides a quantification of the deviations between true species age and phylogenetic age due to incomplete taxon sampling, extinction, and unknown speciation modes. We found that phylogenetic age is a good proxy of species age only in a rather unlikely case in which 1) all species in a clade are known to science and included in the phylogenetic tree, 2) speciation occurs as a strictly bifurcating process, and 3) there is no or little extinction. Using simulations, we identified that incomplete taxon sampling and budding and anagenetic speciation modes cause the highest mismatch between phylogenetic age and true species age and cannot be accounted for in the absence of additional information, for instance, derived from fossil data. In contrast, under a scenario of bifurcating speciation and fully sampled phylogeny, we proposed a probabilistic approach based on the properties of the birth-death process that can drastically improve the accuracy of the estimated species ages by reducing the bias linked with extinction. We note that, even in this case, the robustness of such estimates will be contingent on the accuracy of the estimated speciation and extinction rates and of course of the underlying phylogenetic tree and dating of the branching times. In the light of our findings, we caution against a direct use of branch lengths as proxies for species ages. We recommend the application of our probabilistic approach to correct species ages when assumptions are met. We hope our results will stimulate a discussion about the use of phylogenetic trees in inferring species age and lead to a critical evaluation of the robustness of inferences linking species age with traits, ecological variables, and extinction risks.

**Acknowledgements**

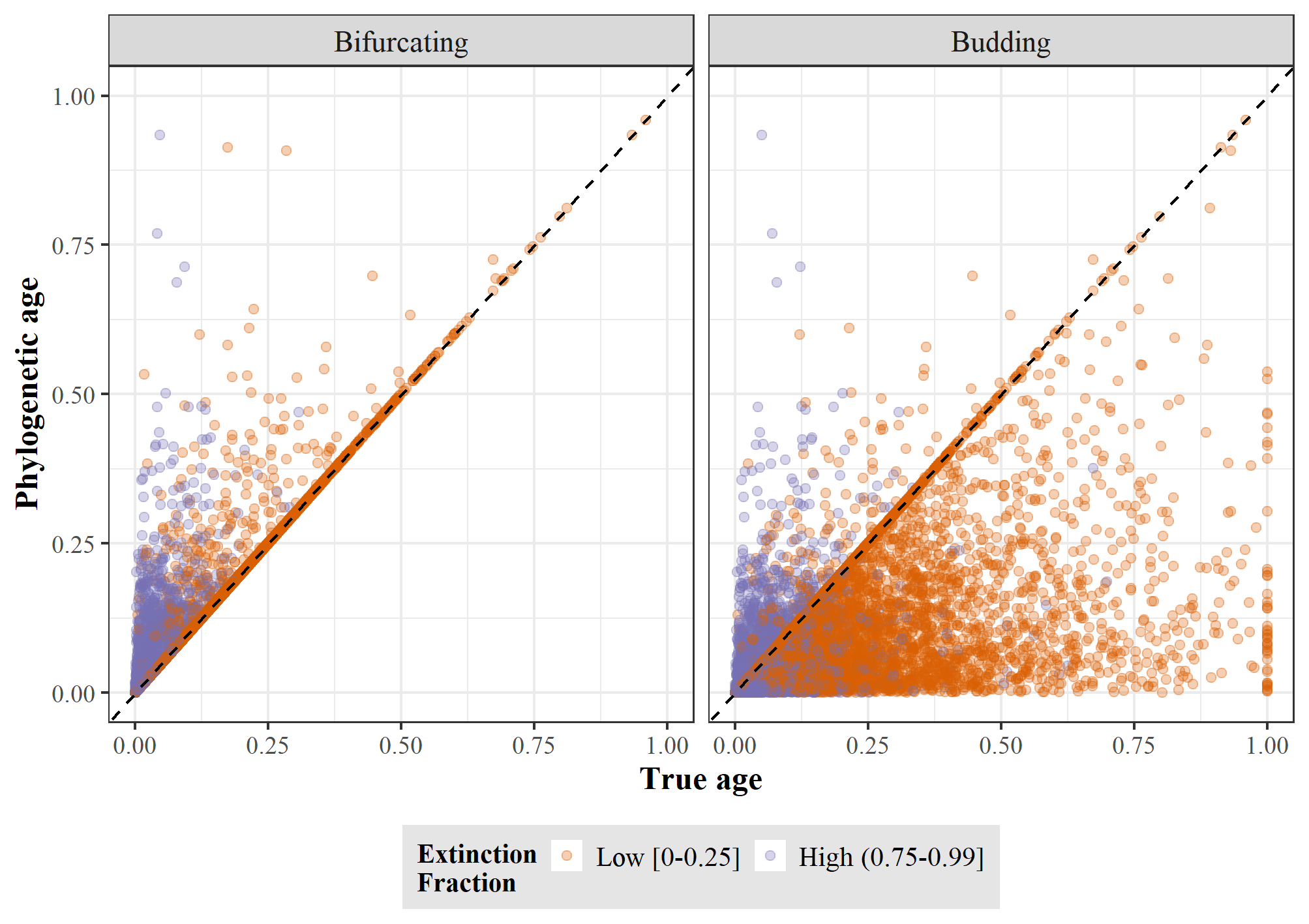
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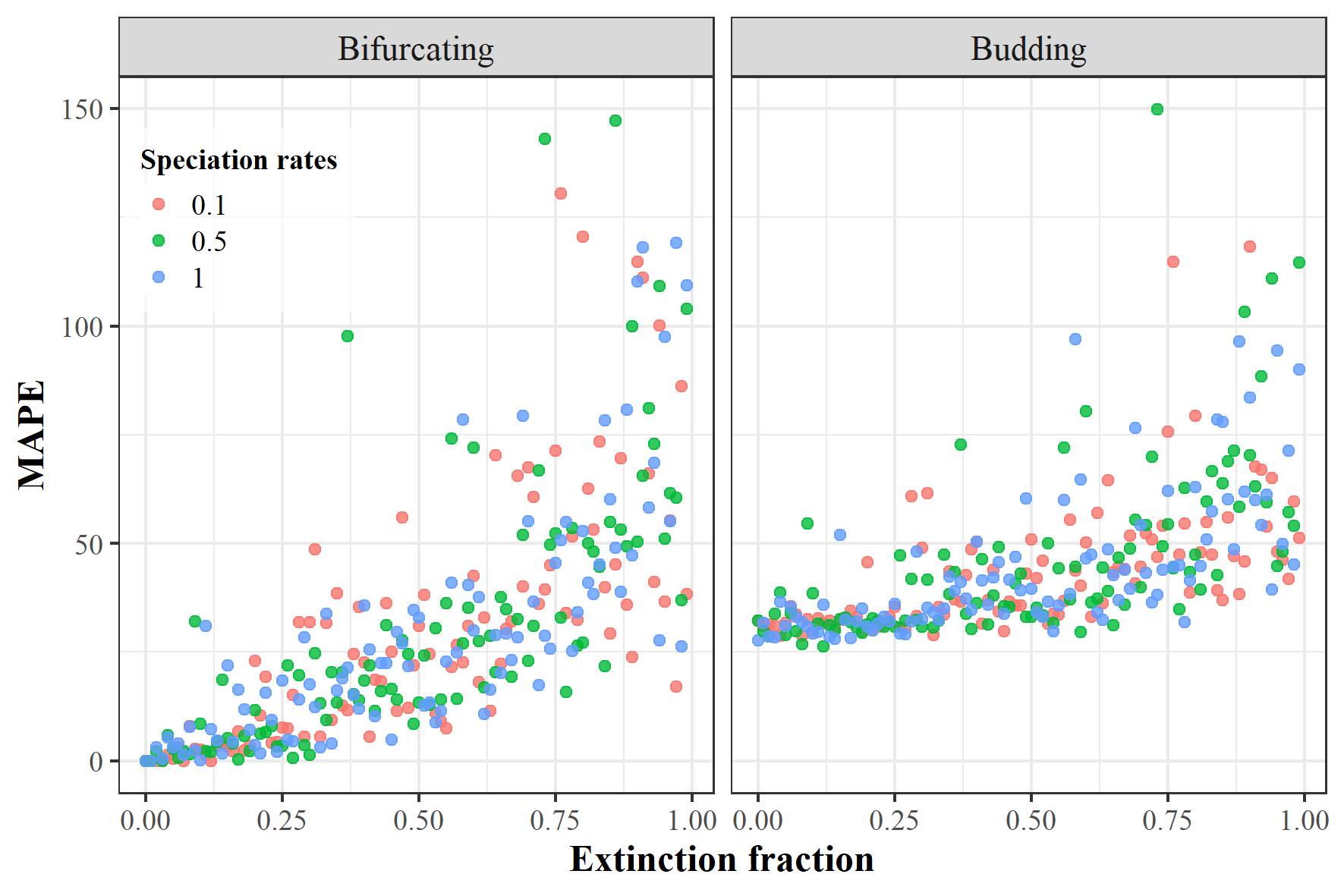
**Fig. 1.** Discrepancy between species ages. Estimations based on the length of the terminal branch in a time-calibrated phylogeny (red) and the first appearance in the fossil record (green). Shark data (*Trianenodon obesus* and *Carcharhinus obscurus*) obtained from Brée et al. (2022). Mammals’ phylogenetic data (except *Homo sapiens*) obtained from Upham et al. (2019). Mammals’ fossil data (except *Homo sapiens*) obtained from Silvestro *et al.* (2018). *Homo sapiens* fossil and phylogenetic data obtained from Callaway (2017) and Rivas-Gonzáles et al. (2023), respectively.



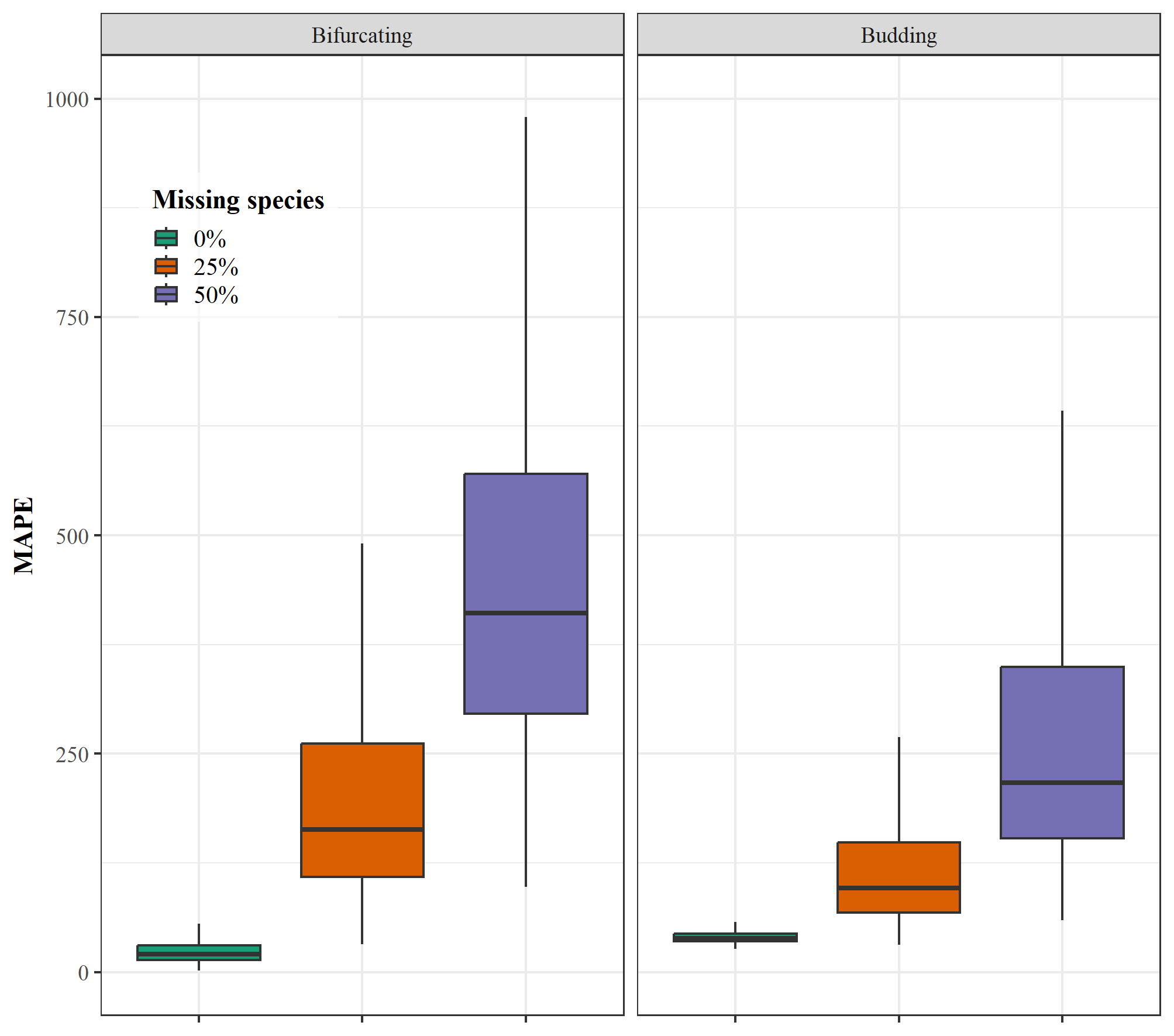
**Fig. 2.** Impact of speciation mode and extinction on species age. For the same hypothetical time-calibrated phylogeny of extant species, the continuation of the same color indicates the same species, solid and dashed lines represent extant and extinct species, respectively, under different speciation modes and extinction scenarios. Numbers display the resulting age of the respective species in million years (myr).



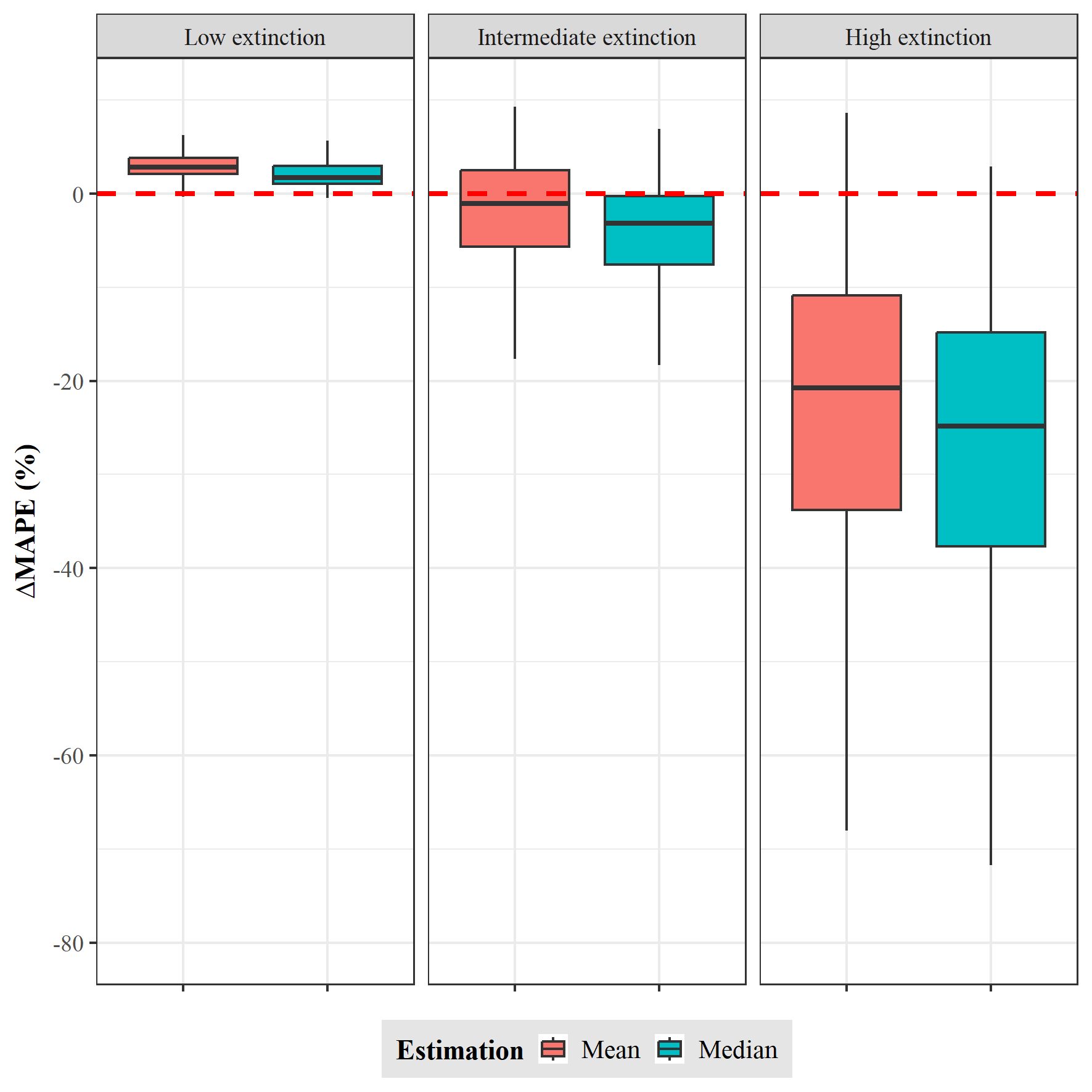
**Fig. 3.** True age versus phylogenetic age at low and high extinction fraction for bifurcating and budding speciation. Each point represents a species and both ages, true and phylogenetic, are scaled to the root age of the correspondent phylogenetic tree.

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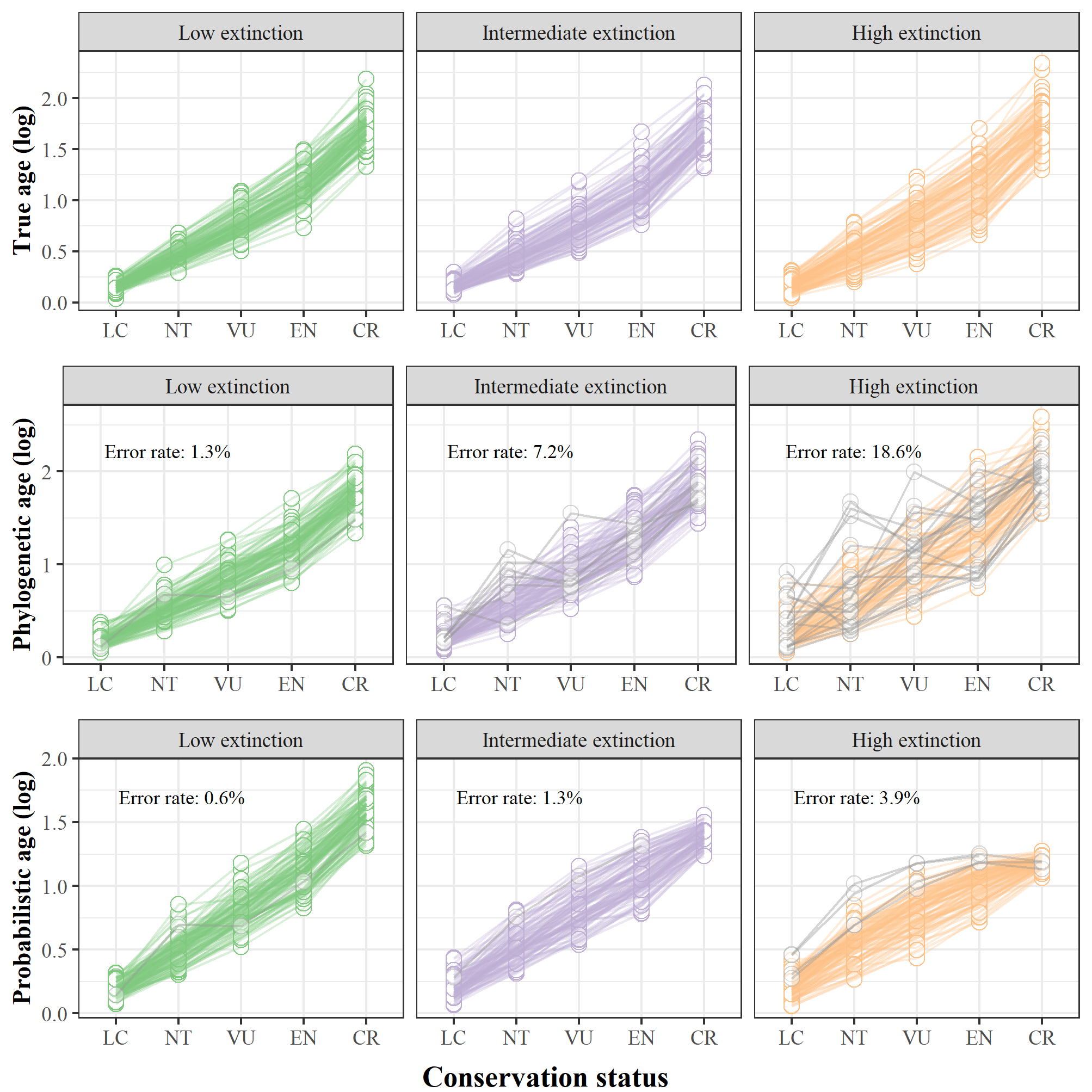
**Fig. 4.** Error in equating phylogenetic age with true age. The error was quantified as mean absolute percentage error (MAPE) between the true and phylogenetic ages across all species for each tree simulated under bifurcating and budding speciation. Each dot represents one replicate of the 300 trees for each speciation mode using different rates of speciation and extinction fraction.



**Fig. 5.** Effect of incomplete taxon sampling on error in species ages. Error in equating the phylogenetic age with true species age for the fully sampled phylogeny, and 25% and 50% of missing extant species, in an intermediate extinction scenario. The error was quantified as mean absolute percentage error (MAPE) between the true phylogenetic ages across 100 species for each of 1000 trees for each missing species scenario simulated under bifurcating and budding speciation.



**Fig. 6.** Performance of the probabilistic age estimator. ΔMAPE for the three extinction scenarios (low, intermediate, and high; from left to right) was quantified as the difference of the mean absolute percentage error (MAPE) of the probabilistic estimator point estimates (mean and median) and the MAPE of the phylogenetic age. The MAPE was quantified as the difference between the true and point estimates (mean and median) of phylogenetic ages for 100 species across 1000 trees for each extinction scenario simulated under bifurcating speciation. The red dashed line represents no difference between the compared MAPEs, negative ΔMAPE values indicate an improvement in the accuracy of the probabilistic estimator over the phylogenetic age.



**Fig. 7.** Power to recover an age extinction-risk relationship. Simulated species ages under three extinction scenarios and assuming bifurcating speciation were binned into conservation status categories, which represents an increase in extinction risk by age (LC = Least Concern; NT = Near Threatened; VU = Vulnerable; EN = Endangered; CR = Critically Endangered). We used the phylogenetic age and the mean age obtained from our probabilistic corrective function to calculate the mean age per conservation status category and assess if every mean age increases in comparison with the previous category with lower extinction risk. The error rate is the percentage across all 1000 phylogenies where the relationship between the mean ages and the conservation status categories is not always increasing (shown by grey lines).

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